MATERIALS MECHANICS ANSWERS OCR A LEVEL YEAR 1

1.

Question		Expected Answers		Additional Guidance		
(a)		elastic potential (energy) / strain (energy)	B1	Note: The candidates do not need to include 'energy' since it is in the stem of the question Not: 'stored energy' / 'elastic energy'		
(b)	(i)	strain = $\frac{0.35 \times 10^{-3}}{1.2}$ = 2.9(2)×10 ⁻⁴	B1			
	(ii)	stress = $1.9 \times 10^{11} \times 2.92 \times 10^{-4}$ (= 5.55×10^{7} Pa) tension = $5.55 \times 10^{7} \times 1.4 \times 10^{-7}$	C1	Possible ecf from b(i)		
		tension = 7.8 (N)	A1	Allow: Bald answer scores 2 marks		
(c)	(i) 1	10 ⁻⁹ (m)	B1			
	(i) 2	Material does not return to original length / shape/ size when the force / stress is removed	B1	There must be reference to stress / force removed to score this mark Note: If there is no reference to unloading then allow 'material is permanently deformed'		
	(ii)	50 times (stronger)	B1			
	(iii)	Less mass / less weight / lighter Stronger / greater tensile strength	B1 B1			
		Total	9			

uesti	on	Expected Answers	Marks	Additional Guidance
(a)		mass = <u>140 × 3.0</u> (= 420 kg)	B1	Allow : $\frac{420}{3.0} = 140$ (reverse argument)
(b)	(i)	total mass = $500 + 560 + 420$ (= 1480 kg) total weight = $1480 \times 9.8(1)$ / total weight = 14520 (N) net force = 1480×1.8 / net force = 2664 (N)	C1 C1 C1	Note: Omitting one of the masses – can score maximum of 3 Omitting two masses – can score maximum of 2 Examples:
		tension = $14520 + 2664$ tension = $1.7(2) \times 10^4$ (N)	C1 A0	3 marks if mass of cable is omitted tension = 1908 +10400 = 1.23×10^4 (N) 2 marks if mass of cable and people are omitted tension = $900 + 4905 = 5.8 \times 10^3$ (N) Note: 4 marks for 'tension = $(m(g+a) =) 1480 \times (9.81 + 1.8)$ '
	(ii)	stress = $\frac{1.72 \times 10^4}{3.8 \times 10^{-4}}$ / stress = $\frac{(b)(i)}{3.8 \times 10^{-4}}$ stress = $4.5(3) \times 10^7$ (Pa)	C1 A1	Possible ecf from (i) Note: A tension of 1.7×10^4 (N) gives an answer of $4.4(7) \times 10^7$ (Pa)
		Total	7	

3.

uestion	Expected Answers		Additional Guidance	
(a)	The graph shows length and not extension of the spring / spring has original length (of 2.0 cm) (AW)	B1	Allow: 'length cannot be zero'	
(b)	Straight line (graph) / linear graph / force ∞ extension / constant gradient (graph)	B1	Not 'force ∝ <u>length'</u>	
(c)	force constant = $\frac{2.0}{0.04}$ force constant = 50 (N m ⁻¹)	C1 A1	Note : The mark is for any correct substitution Allow : 1 mark for 0.5 (N m ⁻¹) $- 10^{n}$ error Allow 1 mark for $5/12 \times 10^{-2} = 41.7$ or $4/10 \times 10^{-2} = 40$ or $3/8 \times 10^{-2} = 37.5$ or $2/6 \times 10^{-2} = 33.3$ or $1/4 \times 10^{-2} = 25$	
(d)	work done = $\frac{1}{2}Fx$ or $\frac{1}{2}kx^2$ or 'area under graph' work done = $\frac{1}{2}\times3.0\times0.06$ or $\frac{1}{2}\times50\times0.06^2$ work done = 0.09 (J)	C1 A1	Possible ecf Note: 1 sf answer is allowed	
(e)	Find the gradient / slope (of the tangent / graph) Maximum speed at 1.0s / 3.0s / 5.0s / steepest 'part' of graph / displacement = 0	B1 B1	Allow:2 marks for 'steepest / maximum gradient'	
	Total	8		

Question		Expected Answers		Additional Guidance	
(a)	(i)	It has maximum / large / increased stress at this point	B1	Allow: it has 'same force but thinner/smaller area' Not: Thin / small area	
	(ii)	The tape has (permanent) extension / deformation when the force / stress is removed (AW)	B1	Note: Need reference to force or stress removed Allow: ' does not return to original size / shape / length when force / stress is removed'	
(b)		Measurement:	B1 B1 X 2	The term diameter to be included and spelled correctly to gathe mark	
		Equipment: Micrometer / vernier (calliper) (for the diameter of the wire) Any two from: Ruler / (metre) rule / tape measure (for measuring the original length / extension) Travelling microscope (for measuring extension) Scales / balance (for measuring the mass & mg	B1 B1 × 2	The term <i>micrometer / vernier</i> (calliper) to be included and spelled correctly to the gain mark. (ALLOW: Micrometer is used to measure area / radius / thickness – as BOD)	
		equation is used or for measuring weight) / Newtonmeter (for the weight of hanging masses) / 'known' weights used		Allow: 'known masses & mg equation' but not 'known masses'	
		Determining Young modulus: stress = force/(cross-sectional) area and strain = extension/original length	B1	Allow: stress = F/A and strain = x/L	
		Young modulus = stress/strain / Young modulus is equal to the gradient from stress-strain graph (in the linear region)	B1	Special case for determining Young modulus: Gradient from force-extension graph is $\frac{EA}{L}$ B1	
		,		Young modulus = gradient \times L/A B1	

5.

a(i)	Y (is brittle)	B1	
a(ii)	(Both) obey Hooke's law	B1	Allow (For both) stress ∝ strain / elastic (behaviour) / 'not plastic (behaviour)' / force ∝ extension Not: 'straight line(s)'
a(iii)	Gradient (of the linear section) is equal to Young Modulus / gradient is largest	B1	Allow: 'slope' for 'gradient'
	X (has largest Young modulus)	В1	
b	(force increases by a factor of) 30^2 force = 240×30^2	C1	
	force = 2.16×10^5 (N)	A1	Allow : 1 mark for value of breaking stress of $1.2(2) \times 10^9$ (Pa)
	Total	6	

Question		on	Answers	Marks	Guidance
6	(a)		The extension ∞ (applied) force (on spring) (as long as the elastic limit is not exceeded)	B1	
	(b)	(i)	Gradient / slope (of line / graph) / force divided by extension The term gradient /slope / divided to be included and spelled correctly to gain the B1 mark	B1	Must use tick or cross on Scoris to show if the mark is awarded
		(ii)	Area (under the graph / line)	B1	Allow: ½ × force × extension Allow: ½ × force constant × extension ² if (b)(i) is correct
	(c)		The extension (for the combination) is doubled Force (for each spring) is the same / constant (force constant = force/extension, hence it is halved)	B1 B1	Allow: 1 mark for 'F is the same, x is doubled' Allow: 2 marks for 'the springs need half the force to give the same (total) extension'
	(d)	(i)	Young modulus = stress/strain As long as the elastic limit is not exceeded / in the linear region of stress against strain graph / Hooke's law is obeyed	M1 A1	
		(ii) 1	stress = $\frac{4.2}{0.20 \times 10^{-6}}$ stress = 2.1×10^{7} (Pa)	C1 A1	Allow: 1 mark for 2.1×10^n , $n \neq 7$
		(ii) 2	Young modulus = $\frac{2.1 \times 10^7}{0.015}$ Young modulus = 1.4×10^9 (Pa)	C1 A1	Possible ecf from (ii)1
		(ii) 3	energy = $\frac{1}{2}Fx$ $x = 0.70 \times 0.015$ / $x = 0.0105$ (m) energy = $\frac{1}{2} \times 4.2 \times (0.70 \times 0.015)$ energy = 2.2×10^{-2} (J)	C1 C1 A1	
			Total	14	

Question	Answer		Guidance
(a)	The graph is a straight line through the <u>origin</u> / F <u>proportional</u> to x / force is <u>proportional</u> to extension	B1	Use ticks on Scoris to show where the marks are awarded \nearrow origin / proportional must be spelled correctly to gain the mark Not: $F \propto X$
(b)	force constant	B1	Allow: spring constant
(c)	stress = $\frac{100}{\pi \times (2.8 \times 10^{-4})^{3}} (= 4.06 \times 10^{8} \text{ Pa})$ strain = $\frac{4.0 \times 10^{-3}}{1.60} (= 2.5 \times 10^{-3})$ $E = \frac{4.06 \times 10^{8}}{2.5 \times 10^{-3}}$ Young modulus = 1.6×10^{11} (Pa)	C1 C1	Allow use of any other point on the graph. Alternative method: $E = \frac{FL}{Ax} \qquad \qquad \text{C1} \text{(Any subject)}$ $E = \frac{100 \times 1.60}{\pi \times (2.8 \times 10^{-4})^2 \times 4.0 \times 10^{-3}} \qquad \text{C1}$ $E = 1.6 \times 10^{11} \text{ (Pa)} \qquad \qquad \text{A1}$ Allow 2 marks for 1.6 × 10°, n ≠ 11 (POT error)
(d)	(Straight line) with quarter gradient Correct reasoning, for example: • gradient = EA/L and A decreases by a factor of 4 • A decreases by a factor of 4 and the same force gives 4 times the extension	B1 B1	Note: No need to define the labels
(e)	1/2 $kx^2 = 1/2 \ mv^2$ Manipulation leading to $v \propto x$, for example: • taking square root of both sides (gives $v \propto x$) • $v^2 \propto x^2$ (hence $v \propto x$) • $v = (\sqrt{k/m})x$ (and therefore $v \propto x$)	M1 A1	Note: No need to define the labels
	Total	9	