

**Circle Theorems Past Paper Questions Edexcel – None Calculator**

1.

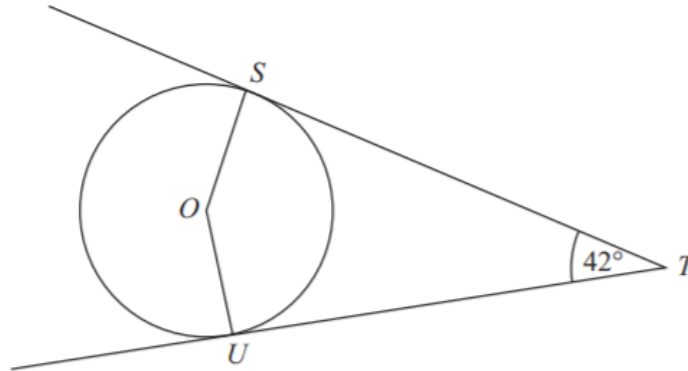


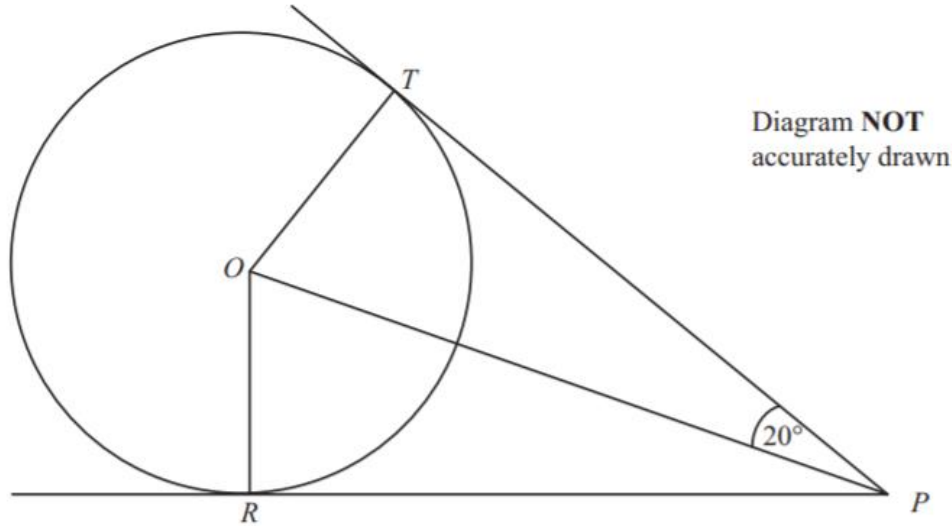
Diagram **NOT**  
accurately drawn

$S$  and  $U$  are points on the circumference of a circle, centre  $O$ .  
 $ST$  and  $UT$  are tangents to the circle.  
Angle  $STU = 42^\circ$

Work out the size of angle  $SOU$ .  
Give reasons for your answer.

2.

i



$T$  and  $R$  are two points on a circle centre  $O$ .

$PT$  and  $PR$  are the tangents to the circle from  $P$ .

Angle  $TPO = 20^\circ$ .

Work out the size of angle  $TOR$ .

You must give reasons for each stage of your working.

3.

i

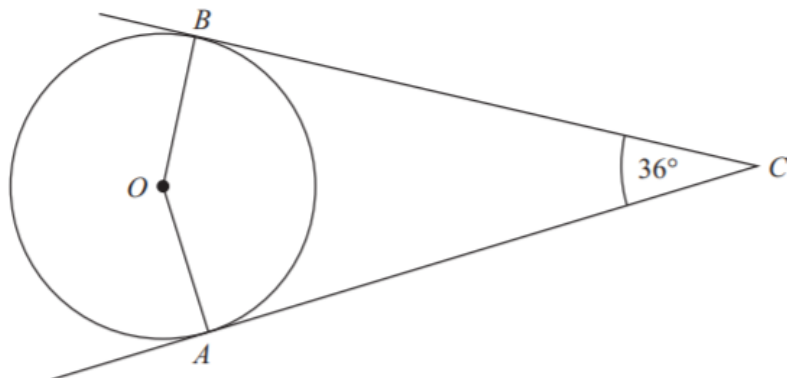


Diagram **NOT**  
accurately drawn

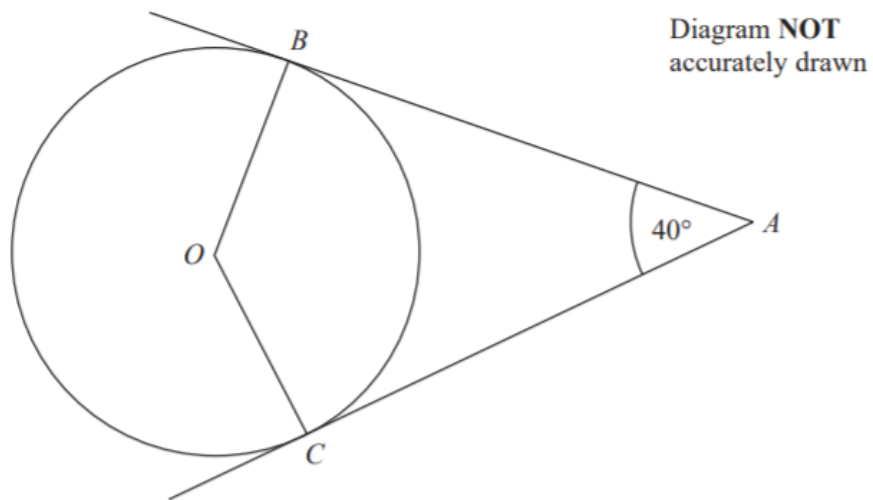
*A* and *B* are points on the circumference of a circle, centre *O*.  
*AC* and *BC* are tangents to the circle.

Angle  $ACB = 36^\circ$ .

Find the size of angle  $OBA$ .  
Give reasons for your answer.

4.

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*B* and *C* are points on the circumference of a circle, centre *O*.  
*AB* and *AC* are tangents to the circle.  
Angle *BAC* =  $40^\circ$ .

Find the size of angle *BCO*.

5.

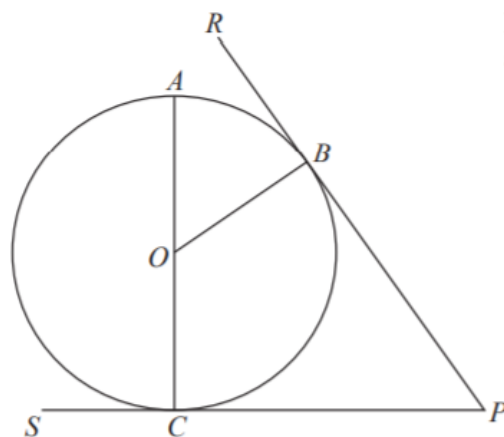


Diagram **NOT**  
accurately drawn

$A$ ,  $B$  and  $C$  are points on a circle, centre  $O$ .

$RBP$  is the tangent to the circle at  $B$ .

$SCP$  is the tangent to the circle at  $C$ .

$AOC$  is a diameter of the circle.

Prove that angle  $AOB$  is equal to angle  $CPB$ .

You must give reasons at each stage.

6.

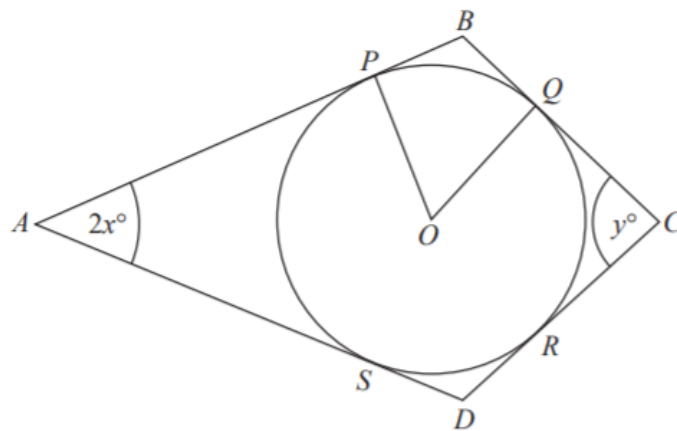


Diagram NOT  
accurately drawn

$P$ ,  $Q$ ,  $R$  and  $S$  are points on the circumference of a circle, centre  $O$ .  
 $APB$ ,  $BQC$ ,  $CRD$  and  $DSA$  are tangents to the circle.  
 $ABCD$  is a kite.

Angle  $PAS = 2x^\circ$

Angle  $QCR = y^\circ$

Find an expression in terms of  $x$  and  $y$  for the size, in degrees, of the angle  $POQ$ .

Give your expression in its simplest form.

Give reasons for your answer.

7.

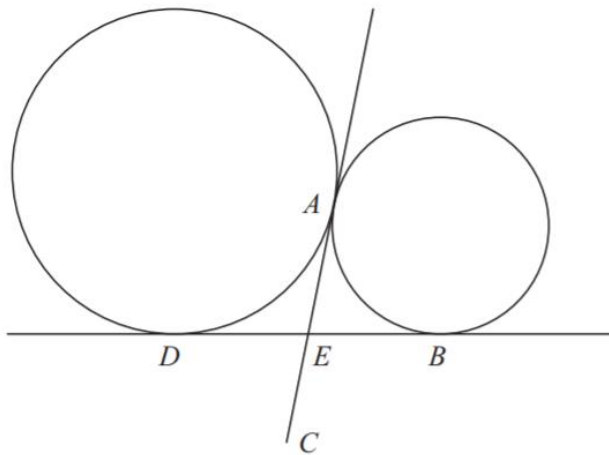


Diagram **NOT**  
accurately drawn.

*A* and *D* are two points on the circumference of a circle.  
*A* and *B* are two points on the circumference of a smaller circle.  
*DB* and *AC* are tangents to both circles.  
*E* is the intersection of *DB* and *AC*.  
*E* is the midpoint of *AC*.

Prove that *ABCD* is a rectangle.

8.

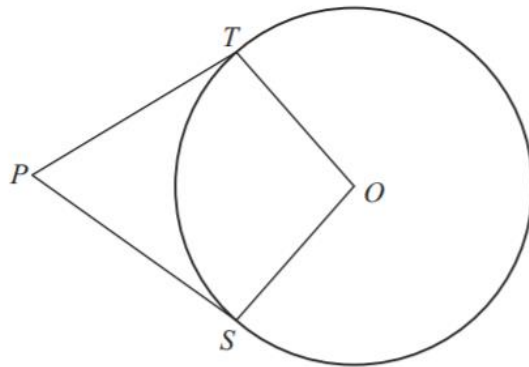


Diagram **NOT**  
accurately drawn

$S$  and  $T$  are points on the circumference of a circle, centre  $O$ .  
 $PT$  and  $PS$  are tangents.  
 Angle  $TPO = 24^\circ$ .

Work out the size of angle  $SOT$ .

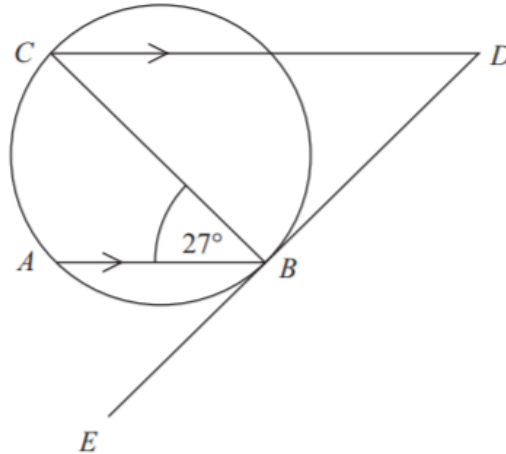
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9.

4

Diagram NOT  
accurately drawn



*A, B and C* are three points on a circle.  
*DBE* is a tangent to the circle.  
*AB* is parallel to *CD*.  
*BC* is a diameter.  
 Angle *ABC* =  $27^\circ$ .

Find the size of angle *CDB*.  
 Give reasons for your answer.

10.

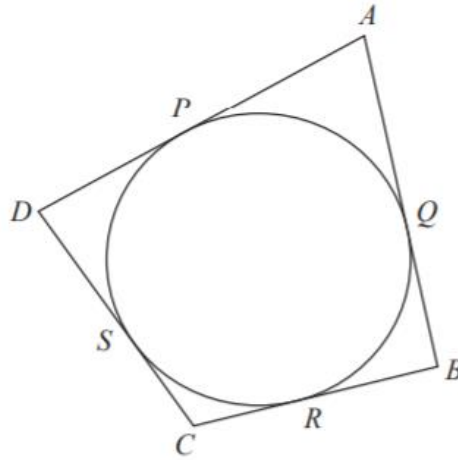


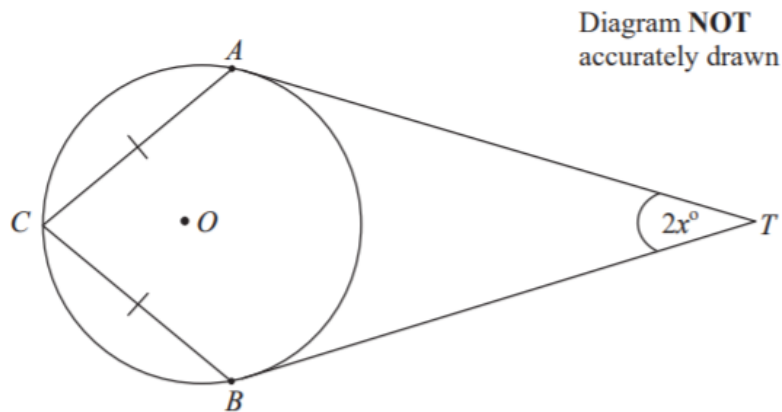
Diagram **NOT**  
accurately drawn

$ABCD$  is a quadrilateral.  
 $AB$ ,  $AD$ ,  $BC$  and  $CD$  are tangents to a circle.  
 The tangents touch the circle at  $Q$ ,  $P$ ,  $R$  and  $S$  respectively.  
 $AC$  goes through the centre of the circle.

$AP : PD$  is in the ratio  $3 : 2$   
 $AQ : QB$  is in the ratio  $3 : 2$

Prove that  $ABCD$  is a kite.

11.



$A$ ,  $B$  and  $C$  are points on the circumference of the circle, centre  $O$ .

$TA$  and  $TB$  are tangents to the circle.

$CA = CB$ .

Angle  $ATB = 2x^\circ$ .

Prove that angle  $ACB = (90 - x)^\circ$ .

12.

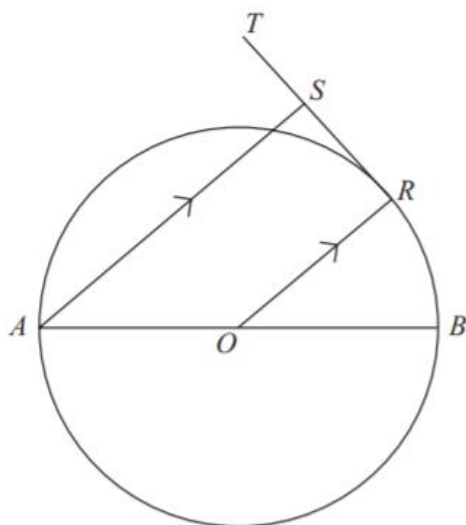


Diagram **NOT**  
accurately drawn

$AB$  is a diameter of a circle centre  $O$ .  
 The point  $R$  is on the circumference of the circle.  
 $RST$  is the tangent to the circle at  $R$ .  
 $AS$  is parallel to  $OR$ .

Prove that the size of angle  $AST$  is  $90^\circ$ .

13.

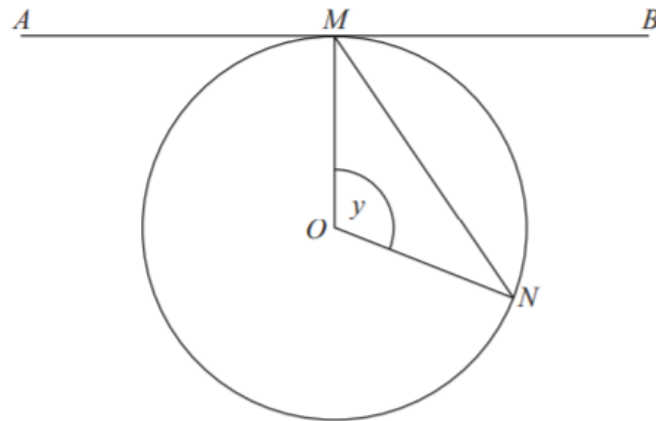


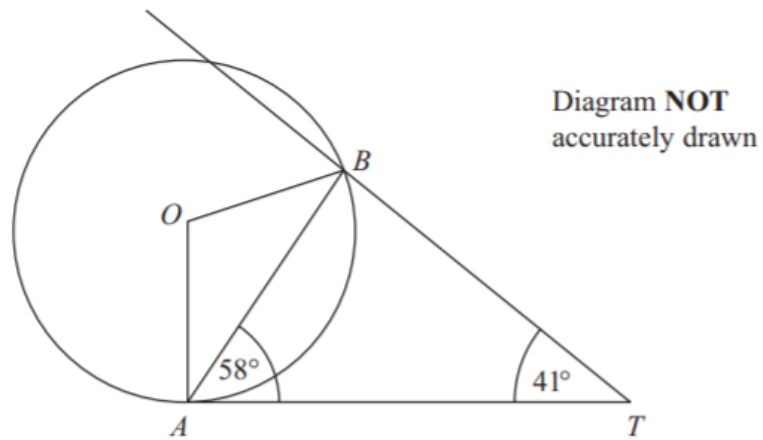
Diagram **NOT**  
accurately drawn

$M$  and  $N$  are two points on the circumference of a circle centre  $O$ .  
The straight line  $AMB$  is the tangent to the circle at  $M$ .

Angle  $MON = y$

Prove that angle  $BMN = \frac{1}{2}y$

14.



$A$  and  $B$  are points on the circumference of a circle, centre  $O$ .

$AT$  is a tangent to the circle.

Angle  $TAB = 58^\circ$ .

Angle  $BTA = 41^\circ$ .

Calculate the size of angle  $OBT$ .

You must give reasons at each stage of your working.

15.

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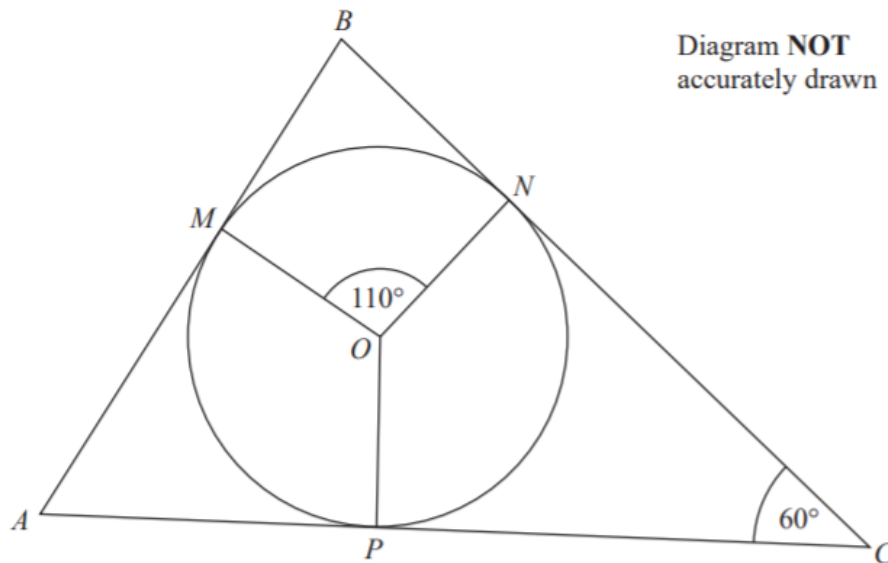


Diagram **NOT**  
accurately drawn

$M$ ,  $N$  and  $P$  are points on the circumference of a circle, centre  $O$ .  
 $AMB$ ,  $BNC$ , and  $CPA$  are tangents to the circle.

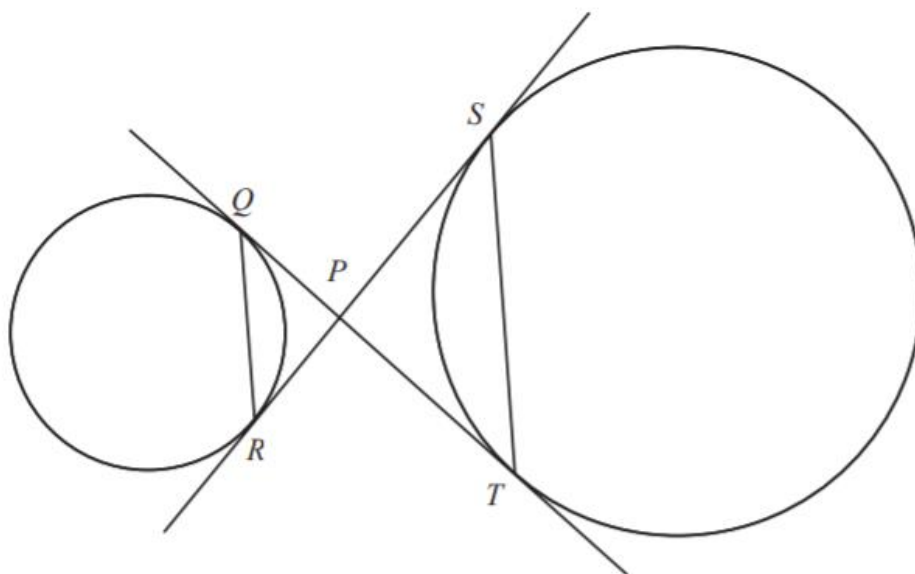
Angle  $MON = 110^\circ$

Angle  $BCA = 60^\circ$

Work out the size of angle  $BAC$ .

Give reasons for each stage of your working.

16.



$Q$  and  $R$  are two points on the circumference of a circle.  
 $S$  and  $T$  are two points on the circumference of another circle.

$QT$  and  $SR$  are tangents to both circles.  
 $P$  is the point of intersection of the two tangents.

Prove that  $QR$  is parallel to  $ST$ .