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Surname	Other names

Pearson Edexcel GCE

Centre Number | Candidate Number

Core Mathematics C1

Advanced Subsidiary

Wednesday 16 May 2018 – Morning

Time: 1 hour 30 minutes

Paper Reference **6663/01**

You must have:
Mathematical Formulae and Statistical Tables (Pink)

Total Marks

Calculators may NOT be used in this examination.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided – *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets – *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶

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1. (i) Simplify

$$\sqrt{48} - \frac{6}{\sqrt{3}}$$

Write your answer in the form $a\sqrt{3}$, where a is an integer to be found.

(2)

(ii) Solve the equation

$$3^{6x-3} = 81$$

Write your answer as a rational number.

(3)

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Question 1 continued

Q1

(Total 5 marks)

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2. Given

$$y = 3\sqrt{x} - 6x + 4, \qquad x > 0$$

(a) find $\int y \, dx$, simplifying each term.

(3)

(b) (i) Find $\frac{dy}{dx}$

(ii) Hence find the value of x such that $\frac{dy}{dx} = 0$

(4)

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Question 2 continued

(Total 7 marks)

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3.

$$f(x) = x^2 - 10x + 23$$

(a) Express $f(x)$ in the form $(x + a)^2 + b$, where a and b are constants to be found.

(2)

(b) Hence, or otherwise, find the exact solutions to the equation

$$x^2 - 10x + 23 = 0$$

(2)

(c) Use your answer to part (b) to find the larger solution to the equation

$$y - 10y^{0.5} + 23 = 0$$

Write your solution in the form $p + q\sqrt{r}$, where p, q and r are integers.

(2)

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Question 3 continued

Q3

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4. Each year, Andy pays into a savings scheme. In year one he pays in £600. His payments increase by £120 each year so that he pays £720 in year two, £840 in year three and so on, so that his payments form an arithmetic sequence.

(a) Find out how much Andy pays into the savings scheme in year ten.

(2)

Kim starts paying money into a different savings scheme at the same time as Andy. In year one she pays in £130. Her payments increase each year so that she pays £210 in year two, £290 in year three and so on, so that her payments form a different arithmetic sequence.

At the end of year N, Andy has paid, in total, twice as much money into his savings scheme as Kim has paid, in total, into her savings scheme.

(b) Find the value of N.

(5)

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Question 4 continued

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Question 4 continued

Q4

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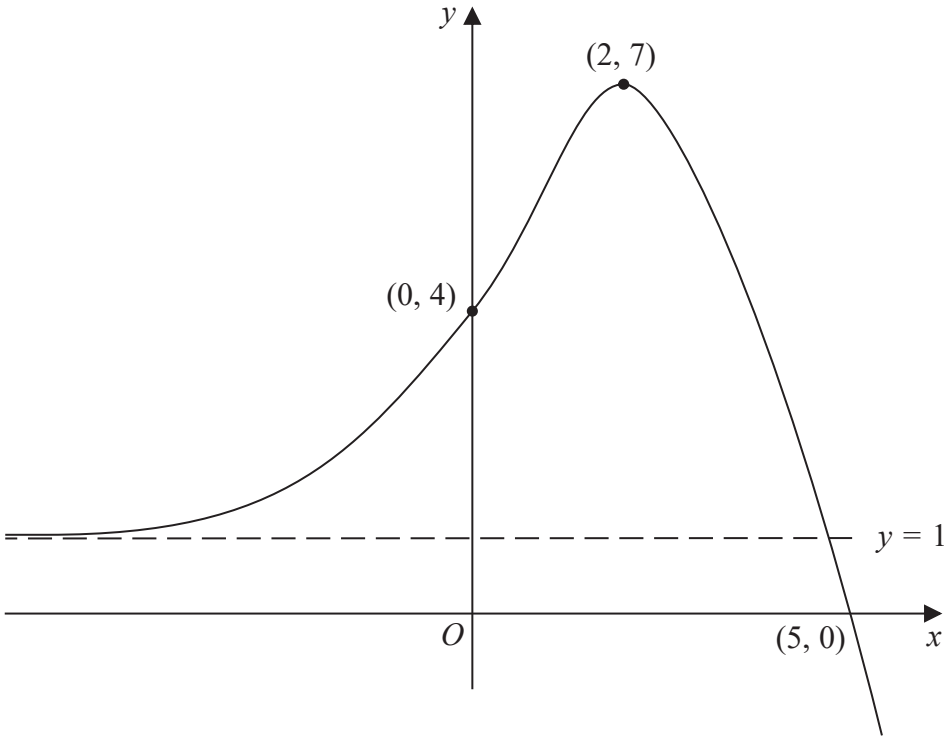

Figure 1

Figure 1 shows the sketch of a curve with equation $y = \mathrm{f}(x)$, $x \in \mathbb{R}$.

The curve crosses the y-axis at (0, 4) and crosses the x-axis at (5, 0).

The curve has a single turning point, a maximum, at (2, 7).

The line with equation $y = 1$ is the only asymptote to the curve.

(a) State the coordinates of the turning point on the curve with equation $y = \mathrm{f}(x - 2)$.
(1)

(b) State the solution of the equation $\mathrm{f}(2x) = 0$
(1)

(c) State the equation of the asymptote to the curve with equation $y = \mathrm{f}(-x)$.
(1)

Given that the line with equation $y = k$, where k is a constant, meets the curve $y = \mathrm{f}(x)$ at only one point,

(d) state the set of possible values for k.
(2)

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Question 5 continued

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Question 5 continued

(Total 5 marks)

Q5

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6. A sequence $a_1, a_2, a_3, \ldots$ is defined by

$$a_1 = 4$$

$$a_{n+1} = \frac{a_n}{a_n + 1}, \qquad n \geqslant 1, n \in \mathbb{N}$$

(a) Find the values of a_2, a_3 and a_4

Write your answers as simplified fractions.

(3)

Given that

$$a_n = \frac{4}{pn + q}, \text{ where } p \text{ and } q \text{ are constants}$$

(b) state the value of p and the value of q.

(2)

(c) Hence calculate the value of N such that $a_N = \frac{4}{321}$

(2)

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Question 6 continued

Q6

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7. The equation $20x^2 = 4kx - 13kx^2 + 2$, where k is a constant, has no real roots.

(a) Show that k satisfies the inequality

$$2k^2 + 13k + 20 < 0$$

(4)

(b) Find the set of possible values for k.

(4)

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Question 7 continued

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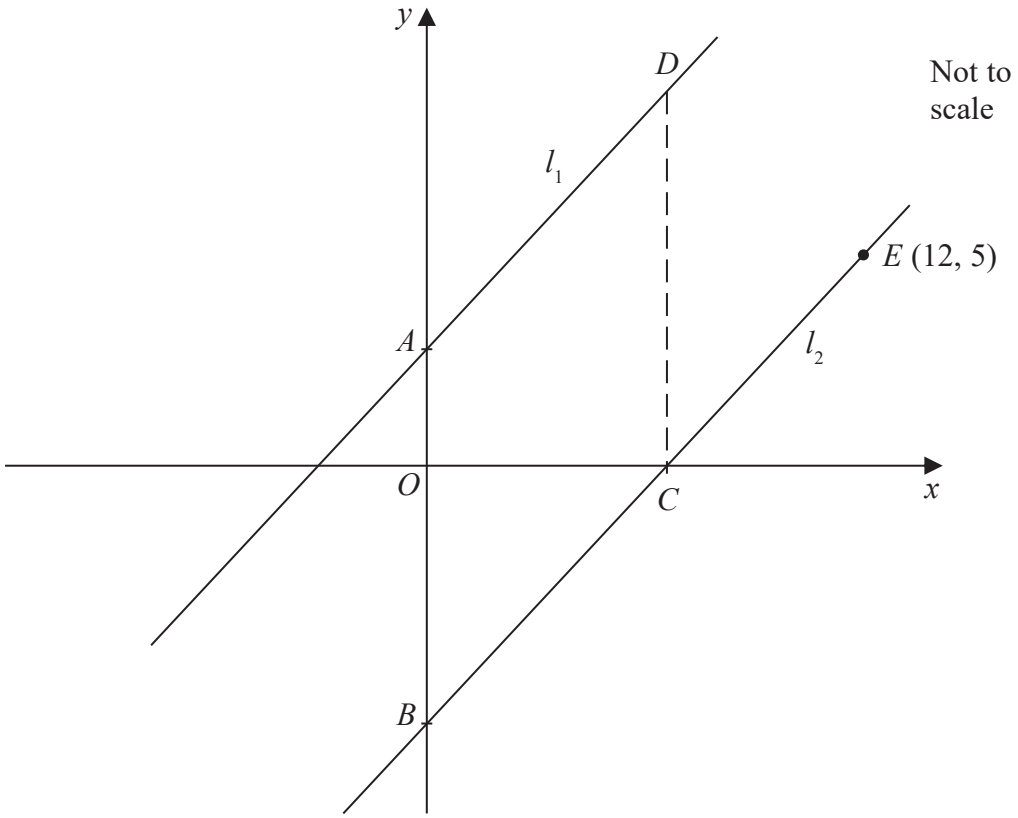

Figure 2

Figure 2 shows the straight line l_1 with equation $4y = 5x + 12$

(a) State the gradient of l_1

(1)

The line l_2 is parallel to l_1 and passes through the point E (12, 5), as shown in Figure 2.

(b) Find the equation of l_2. Write your answer in the form $y = mx + c$, where m and c are constants to be determined.

(3)

The line l_2 cuts the x-axis at the point C and the y-axis at the point B.

(c) Find the coordinates of

(i) the point B,

(ii) the point C.

(2)

The line l_1 cuts the y-axis at the point A.

The point D lies on l_1 such that $ABCD$ is a parallelogram, as shown in Figure 2.

(d) Find the area of $ABCD$.

(2)

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Question 8 continued

Q8

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9. The curve C has equation $y = \mathrm{f}(x)$, where

$$\mathrm{f}'(x) = (x - 3)(3x + 5)$$

Given that the point P (1, 20) lies on C,

(a) find $\mathrm{f}(x)$, simplifying each term.

(5)

(b) Show that

$$\mathrm{f}(x) = (x - 3)^2(x + A)$$

where A is a constant to be found.

(3)

(c) Sketch the graph of C. Show clearly the coordinates of the points where C cuts or meets the x-axis and where C cuts the y-axis.

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Question 9 continued

Q9

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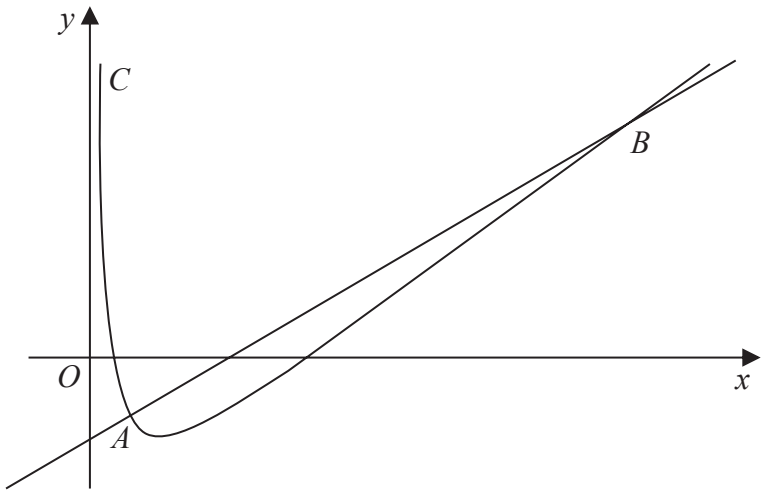

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Figure 3

Figure 3 shows a sketch of part of the curve C with equation

$$y = \frac{1}{2}x + \frac{27}{x} - 12, \qquad x > 0$$

The point A lies on C and has coordinates $\left(3, -\frac{3}{2}\right)$.

(a) Show that the equation of the normal to C at A can be written as $10y = 4x - 27$

(5)

The normal to C at A meets C again at the point B, as shown in Figure 3.

(b) Use algebra to find the coordinates of B.

(5)

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Question 10 continued

Q10

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