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| Pearson Edexcel GCE | Centre Number | Candidate Number |
| Core Mat Advanced Subsid | | s C1 |
| | | |
| Wednesday 17 May 201 Time: 1 hour 30 minute | • | Paper Reference 6663/01 |

Calculators may NOT be used in this examination.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 - there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.

Information

- The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
 - use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ▶



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| 1. Find $\int \left(2x^5 - \frac{1}{4x^3} - 5\right) dx$ | |
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| giving each term in its simplest form. | (4) |
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| $y = \sqrt{x} + \frac{4}{x} + 4$ | x > 0 |
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2. Given

find the value of $\frac{dy}{dx}$ when x = 8, writing your answer in the form $a\sqrt{2}$, where a is a rational number. (5)

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3. A sequence $a_1, a_2, a_3,...$ is defined by

$$a_1 = 1$$

$$a_{n+1} = \frac{k(a_n + 1)}{a_n}, \qquad n \geqslant 1$$

where k is a positive constant.

(a) Write down expressions for a_2 and a_3 in terms of k, giving your answers in their simplest form.

(3)

Given that $\sum_{r=1}^{3} a_r = 10$

(b) find an exact value for k.

(3)





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| 4. | A company, which is making 140 bicycles each week, plans to increase its production. The number of bicycles produced is to be increased by d each week, starting from 140 in week 1, to $140 + d$ in week 2, to $140 + 2d$ in week 3 and so on, until the company is producing 206 in week 12. |
|----|--|
| | (a) Find the value of d . (2) |
| | After week 12 the company plans to continue making 206 bicycles each week. |
| | (b) Find the total number of bicycles that would be made in the first 52 weeks starting from and including week 1. |
| | (5) |
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- $f(x) = x^2 8x + 19$
 - (a) Express f(x) in the form $(x + a)^2 + b$, where a and b are constants.

(2)

The curve C with equation y = f(x) crosses the y-axis at the point P and has a minimum point at the point Q.

(b) Sketch the graph of C showing the coordinates of point P and the coordinates of point Q.

(3)

(c) Find the distance PQ, writing your answer as a simplified surd.

(3)



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6. (a) Given $y = 2^x$, show that

$$2^{2x+1} - 17(2^x) + 8 = 0$$

can be written in the form

$$2y^2 - 17y + 8 = 0$$

(2)

(b) Hence solve

$$2^{2x+1} - 17(2^x) + 8 = 0$$

(4)

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7. The curve C has equation y = f(x), x > 0, where

$$f'(x) = 30 + \frac{6 - 5x^2}{\sqrt{x}}$$

Given that the point P(4, -8) lies on C,

(a) find the equation of the tangent to C at P, giving your answer in the form y = mx + c, where m and c are constants.

(4)

(b) Find f(x), giving each term in its simplest form.

(5)

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Figure 1

The straight line l_1 , shown in Figure 1, has equation 5y = 4x + 10

The point P with x coordinate 5 lies on l_1

The straight line l_2 is perpendicular to l_1 and passes through P.

(a) Find an equation for l_2 , writing your answer in the form ax + by + c = 0 where a, b and c are integers.

(4)

The lines l_1 and l_2 cut the x-axis at the points S and T respectively, as shown in Figure 1.

(b) Calculate the area of triangle SPT.

(4)



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- 9. (a) On separate axes sketch the graphs of
 - (i) y = -3x + c, where c is a positive constant,

(ii)
$$y = \frac{1}{x} + 5$$

On each sketch show the coordinates of any point at which the graph crosses the *y*-axis and the equation of any horizontal asymptote.

(4)

Given that y = -3x + c, where c is a positive constant, meets the curve $y = \frac{1}{x} + 5$ at two distinct points,

(b) show that $(5 - c)^2 > 12$

(3)

(c) Hence find the range of possible values for c.

(4)

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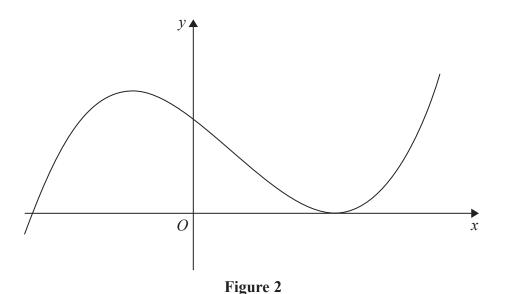


Figure 2 shows a sketch of part of the curve $y = f(x), x \in \mathbb{R}$, where

$$f(x) = (2x - 5)^2(x + 3)$$

- (a) Given that
 - (i) the curve with equation y = f(x) k, $x \in \mathbb{R}$, passes through the origin, find the value of the constant k,
 - (ii) the curve with equation y = f(x + c), $x \in \mathbb{R}$, has a minimum point at the origin, find the value of the constant c.

(3)

(b) Show that $f'(x) = 12x^2 - 16x - 35$

(3)

Points A and B are distinct points that lie on the curve y = f(x).

The gradient of the curve at A is equal to the gradient of the curve at B.

Given that point A has x coordinate 3

(c) find the x coordinate of point B.

(5)

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